

QP CODE: 19101898



Reg No :

Name :

B.Sc.DEGREE (CBCS) EXAMINATION, MAY 2019

Second Semester

B.Sc Electronics Model III

**Complementary Course - MM2CMT07 - MATHEMATICS-LINEAR ALGEBRA AND
DIFFERENTIAL EQUATIONS**

2017 ADMISSION ONWARDS

EBF35514

Maximum Marks: 80

Time: 3 Hours

Part A

Answer any ten questions.

Each question carries 2 marks.

1. Find the dimension of the vector space spanned by $(1,2,0)$ and $(1,3,0)$ in \mathbb{R}^3 .
2. Find the standard matrix for the transformation T where $T(x,y)=(x+y,x-y)$
3. Find skew Hermitian matrix of
$$\begin{bmatrix} 3i & -3 + 4i & 4 - 5i \\ -3 + 4i & -4i & 5 + 6i \\ -4 - 5i & -5 + 6i & 0 \end{bmatrix}$$
4. Define minor.
5. Define eigen values of a matrix.
6. State Cayley Hamilton theorem.
7. Write the nature of characteristic roots of skew-Hermitian matrix.
8. What do you mean by an exact differential equation? Explain.
9. Write down the Bernoulli's Equation. Give an example.
10. Define a partial differential equation with an example.
11. Solve the differential equation $dx=dy=dz$.
12. Explain the terms of a linear partial differential equation $Pp+Qq=R$

(10×2=20)

Part B

Answer any six questions.

Each question carries 5 marks.

13. Define vector subspace.





14. Show that $A = \frac{1}{3} \begin{bmatrix} 1 - 2i & 2i \\ -2i & -1 - 2i \end{bmatrix}$ is unitary
15. Explain normal form or first canonical form of the matrix .
16. Find the characteristic equation of $A = \begin{bmatrix} 1 & 2 & 3 \\ 0 & -4 & 2 \\ 0 & 0 & 7 \end{bmatrix}$
17. Find the eigen vector of the matrix $A = \begin{bmatrix} 4 & -5 \\ 1 & -2 \end{bmatrix}$
18. Solve the initial value problem $\frac{dy}{dx} = \frac{-y}{x}, y(4)=3$
19. Solve $(\frac{dy}{dx})^2 + \frac{dy}{dx}x + \frac{dy}{dx}y + xy = 0$
20. If $z = x+y+f(xy)$ then form the partial differential equation for the surface.
21. Find the integral curve of the equation $\frac{dx}{y+zx} = \frac{dy}{-(x+yz)} = \frac{dz}{x^2-y^2}$

(6×5=30)

Part C

Answer any **two** questions.

Each question carries **15** marks.



22. (a) Write the standard basis of $M_{2 \times 2}$.
 (b) Find the matrix representation for the linear transformation $T: M_{2 \times 2} \rightarrow M_{2 \times 2}$ defined by T
 $\begin{bmatrix} a & b \\ c & d \end{bmatrix} = \begin{bmatrix} a + 2b + 3c & 2b - 3c + 4d \\ 3a - 4b - 5d & 0 \end{bmatrix}$ using standard basis
23. Reduce the normal form and find the rank of the matrix $\begin{bmatrix} 1 & 1 & 1 & 1 \\ 1 & 2 & 3 & 4 \\ 4 & 3 & 2 & 1 \end{bmatrix}$
24. Check whether the consistency of equations,
 $x+y+z=3$
 $x+2y+3z=4$
 $x+4y+9z=6$
25. Solve the initial value problem $(1+x^2) \frac{dy}{dx} + 4xy = x, y(2)=1$

(2×15=30)

